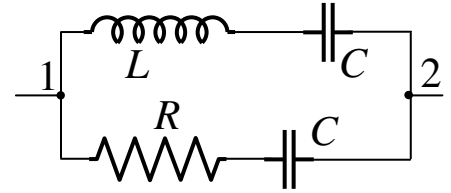


Find $z(\omega)$. This circuit has two branches (top and bottom), each of which has two parts. Each element can be treated like a resistor for purposes of finding impedance:



$$z_{top} = i\omega L - \frac{1}{\omega C} i = \frac{\omega^2 LC - 1}{\omega C} i$$

$$z_{bottom} = R - \frac{1}{\omega C} i = \frac{R\omega C - i}{\omega C}$$

Combining these in parallel:

$$\frac{1}{z_{total}} = \frac{1}{z_{top}} + \frac{1}{z_{bottom}} \qquad \frac{1}{z_{total}} = \frac{\omega C}{(\omega^2 LC - 1)i} + \frac{\omega C}{R\omega C - i}$$

Use a complex conjugate:

$$\frac{1}{z_{total}} = \frac{-\omega Ci}{(\omega^2 LC - 1)} + \left[\frac{\omega C}{R\omega C - i} \right] \left[\frac{R\omega C + i}{R\omega C + i} \right]$$

$$\frac{1}{z_{total}} = \frac{-\omega Ci}{(\omega^2 LC - 1)} + \frac{R\omega^2 C^2}{R^2 \omega^2 C^2 + 1} + \frac{\omega Ci}{R^2 \omega^2 C^2 + 1}$$

Common denominator:

$$\frac{1}{z_{total}} = \frac{(R^2 \omega^2 C^2 + 1)(-\omega Ci) + (R\omega^2 C^2 + \omega Ci)(\omega^2 LC - 1)}{(\omega^2 LC - 1)(R^2 \omega^2 C^2 + 1)}$$

Flip it over:

$$z_{total} = \frac{(\omega^2 LC - 1)(R^2 \omega^2 C^2 + 1)}{(R^2 \omega^2 C^2 + 1)(-\omega Ci) + (R\omega^2 C^2 + \omega Ci)(\omega^2 LC - 1)}$$

Obviously, this could be simplified more. Also, in hindsight, it probably would have been advisable to do this all in Euler (“exponential”) notation.

Here are some numerical values: Given $\omega = 377$ rad/s (standard ω for AC power)
 $L = 2$ H
 $R = 150 \Omega$
 $C = 1 \times 10^{-5}$ F

Then

$$z_{total} = 494.56 - 248.13i \Omega$$

$$\theta = -26.6^\circ$$

$$|z_{total}| = 553.3 \Omega$$