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**LAB #1**  
MATH 345 - NUMERICAL ANALYSIS I  
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Suppose that you need a loan in the amount of  $P = 210,000$  that will be paid over  $m = 30$  years at an annual interest rate  $i \in [10^{-5}, 0.2]$ . The amount that you can afford to repay the loan is a monthly amount of  $A = 1,200$ . It can be shown (you do not have to show this) that  $P, m, A$  and  $i$  are related by the equation

$$P = \frac{A}{(i/12)} \left[ 1 - \left( 1 + \frac{i}{12} \right)^{-12m} \right].$$

Find an approximation  $i^*$  to the interest rate  $i$  using the Bisection method. Find  $i^*$  so that

$$|i - i^*| < 10^{-15}$$

and write out  $i^*$  using 12 decimal places. How many iterations of the Bisection algorithm are needed to compute  $i^*$ ?