15 how much he exceeded I did not know.

¹⁶How much did one brother exceed the other?

¹⁷When you perform (the operations), multiply the area by two, (and the result is)

¹⁸⁻¹⁹The reciprocal of 6, 30 is not obtainable. What should I put to 6, 30 which will give me 22, 45, 0? Put 3, 30, (which is)

²⁰the upper width. Take the reciprocal of 6, the brothers, (and) [multiply] the

(resulting) 0; 10 by 6, 30, and (the resulting) ²¹1, 5 (is) the length which each too[k.....] ²²35 GAR is the breadth. 35 [from 3, 30...... ²³35 from 2,5[5

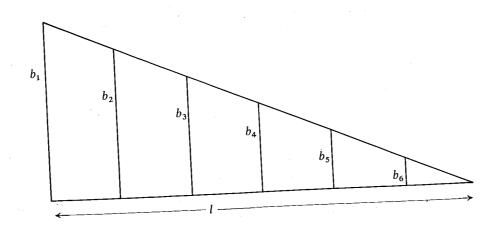
²⁴35 from 2, 2[0

²⁷subtract 35, and the width (?) [.......

We have here one of the 'inheritance' problems which require the partition of property to be distributed among a given number of brothers. The field in question is of triangular shape with length l and area A:

$$l = 6,30$$
 $A = 11,22,30$.

This area is divided among 6 brothers by equidistant lines parallel to the base of the triangle. The question asked by the text concerns the difference between the allotments of the brothers.



(d) YBC 6967

³⁻⁵ As for you—halve 7, by which the *igibūm* exceeded the *igūm*, and (the result is) 3; 30.

⁶⁻⁷Multiply together 3; 30 with 3; 30, and (the result is) 12; 15.

⁸To 12; 15, which resulted for you,

⁹add [1, 0, the produ]ct, and (the result is) 1, 12; 15.

¹⁰What is [the square root of 1], 12; 15? (Answer:) 8; 30.

11 Lay down [8; 30 and] 8; 30, its equal, and then (Reverse)

1-2 subtract 3; 30, the takīltum, from the one,

³add (it) to the other.

⁴One is 12, the other 5.

512 is the igibum, 5 the igum.

Commentary

The problem treated here belongs to a well-known class of quadratic equations characterized by the terms igi and igi-bi (in Akkadian, igūm and igibūm, respectively). These terms refer to a pair of numbers which stand in the relation to one another of a number and its reciprocal, to be understood in the most general sense as numbers whose product is a power of 60. We must here assume the product

$$(1) xy = 1,0$$

as the first condition to which the unknowns x and y are subject. The second condition is explicitly given as

$$x - y = 7.$$

From these two equations it follows that x and y can be found from

$$\begin{cases} x \\ y \end{cases} = \sqrt{\left(\frac{7}{2}\right)^2 + 1, 0} \pm \frac{7}{2},$$

a formula which is followed exactly by the text, leading to

$$\begin{cases} x \\ y \end{cases} = \sqrt{1,12;15} \pm 3;30 = 8;30 \pm 3;30 = \begin{cases} 12 \\ 5 \end{cases}$$

(e) YBC 4662

 24 A ki-lá. $7\frac{1}{2}$ SAR is the area, 45 SAR the volume; one-seventh

²⁵ of that by which the length exceeded the width is its depth. What are the length, the width, and its depth?

 26 When you perform (the operations), take the reciprocal of $7\frac{1}{2}$ SAR, the area, [multiply by] 45, [the volume, (and)]

²⁷you will get its depth. Halve the one-seventh which has been assumed, (and) ²⁸you will get 3; 30. Take the reciprocal of its depth, (and) you will get 0; 10;

²⁹multiply 0; 10 by 45 (SAR), the volume, (and) you will get 7; 30.

³⁰⁻³¹Halve 3; 30, (and) you will get 1; 45; multiply together 1; 45 times 1; 45, (and) you will get 3; 3, 45; add 7; 30 to 3; 3, 45, (and)

¹[The igib]ūm exceeded the igūm by 7.

²What are [the igūm and] the igibūm?