

Magnetic Field due to Current in a Pipe

A uniform current density J flows along a thick-walled copper pipe with inner radius a and outer radius b .
What is the formula for the magnetic field at radius r
(for **any** r)?

$$r < a \rightarrow i_{\text{enc}} = 0 \rightarrow B = 0$$

$$r > b \rightarrow i_{\text{enc}} = J\pi(b^2 - a^2)$$

$$B = \frac{\mu_0}{2\pi r} J\pi(b^2 - a^2)$$

$$a < r < b \rightarrow$$

$$J = \frac{i_{\text{enc}}}{\pi(r^2 - a^2)}$$

$$B2\pi r = \mu_0 i_{\text{enc}} = \mu_0 J\pi(r^2 - a^2)$$

$$B = \mu_0 J \frac{(r^2 - a^2)}{2r}$$

